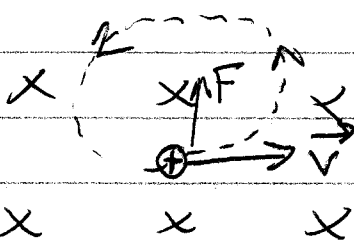


$$F = q\mathbf{v} \times \mathbf{B}$$

Review:

x x x  $B_{in}$



$$F = ?$$

$\oplus$  particle "orbits" CCW when viewed along  $\mathbf{B}$

②

## Induced EMF

$$\mathcal{E} = -\frac{\Delta \Phi_B}{\Delta t}$$

EMF is caused by changing magnetic flux

What is flux? "Total amount" of  $B$  pointing through a coil.

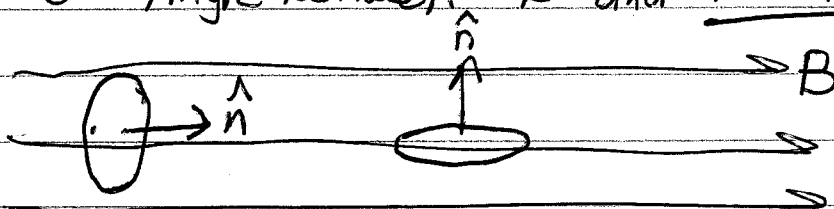
$$\Phi_B = NBA \cos \theta \quad \text{Total flux of coil}$$

$N$  = # of turns of wire

$B$  = mag field strength?

$A$  = Area of coil ( $A = \pi r^2$ )

$\theta$  = Angle between  $\vec{B}$  and normal ( $\hat{n}$ )



$$\theta = 0$$

$$\cos \theta = 1$$

$$\Phi = NBA$$

$$\theta = 90^\circ$$

$$\cos \theta = 0$$

$$\Phi = 0$$

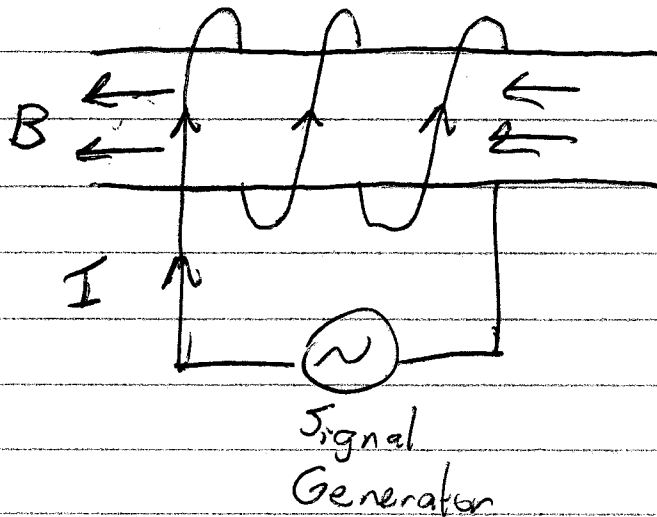
How can we change  $\Phi_B$ ?

- Change  $B$  - move a magnet into place  
- change current in coil
- Change  $\theta$  - rotate the coil
- Change  $A$  - move one edge of coil



$$\mathcal{E} = Bvl$$

3



$I$  is changing but known  
 $I$  causes magnetic field

$$B = \mu_0 N I / l$$

$B$  forms flux in coil

$$\Phi_B = N B A \cos \theta = \underbrace{\mu_0 N^2 A / l}_{L} I$$

$L =$  Inductance in henries (H)

$$\Phi_B = L I$$

Change  $I \rightarrow$  changes  $\Phi \rightarrow$  makes  $\mathcal{E}$

This is an inductor.

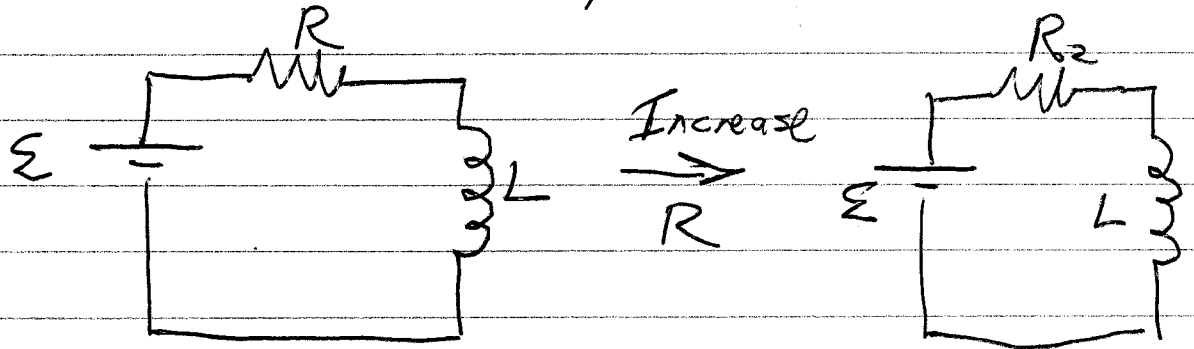
$$\mathcal{E} = \frac{\Delta \Phi}{\Delta t} = \frac{\Delta (L I)}{\Delta t} = L \frac{\Delta I}{\Delta t}$$

④

Lenz's Law - tells us direction of  $\mathcal{E}$ .

Coils hate change.

- Try to decrease  $I$  in an inductor. The coil reacts by trying to boost the current back up to its old value.



$$I = \frac{V_R}{R} = \frac{\mathcal{E}}{R}$$

$$I = \frac{V_R}{R_2}$$

Same  $I$  }  $V_R$  must  
Bigger  $R$  } be bigger

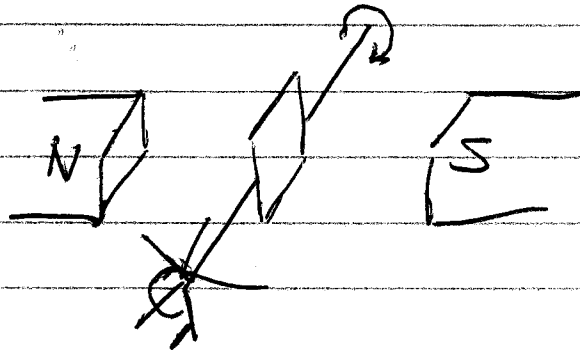
$$\mathcal{E} = V_R + V_L$$

$$V_R = \mathcal{E} - V_L \Rightarrow V_L \text{ must be big}$$

"Inductive Kick" - motor briefly generates high voltage when shut off.

5

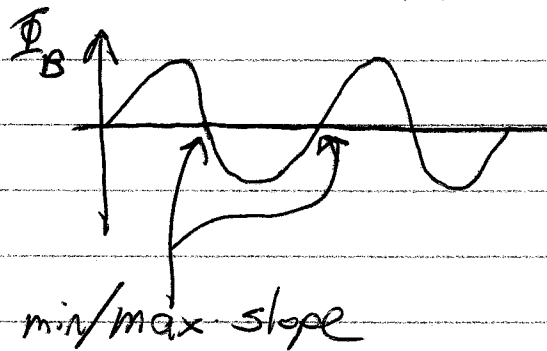
## Electric Generators



Maximum Flux in coil  $\Phi_{\max} = NBA$

Spinning changes  $\ominus$

Minimum Flux  $\Phi_{\min} = -NBA$



$$\mathcal{E} = -\frac{\Delta\Phi}{\Delta t}$$

$$\mathcal{E}_{\max} = NBA \omega$$

$\omega$  = angular speed in radians per second.

$$1 \text{ RPM} \rightarrow \omega = \frac{2\pi}{(60\text{s})} = 0.105 \text{ s}^{-1}$$

$$\text{Ex: } B = 0.004 \text{ T}$$

$$A = 0.0013 \text{ m}^2 \quad (20\text{m radius})$$

$$N = 130$$

$$\omega = 3600 \text{ RPM} \left( \frac{0.105 \text{ s}^{-1}}{1 \text{ RPM}} \right) = 377 \text{ s}^{-1}$$

$$\mathcal{E}_{\max} = 0.25 \text{ V}$$