

Phys 1402 2016-10-13 Lec 15

HW4a is posted - Don't wait!

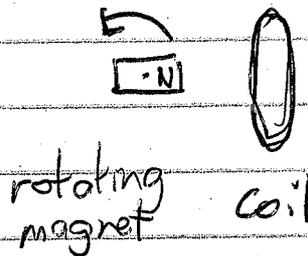
Faraday's Law - Voltage generated by a coil.

$$\mathcal{E} = - \frac{\Delta \Phi_B}{\Delta t}$$

$$\Phi_B = NBA \cos \theta$$

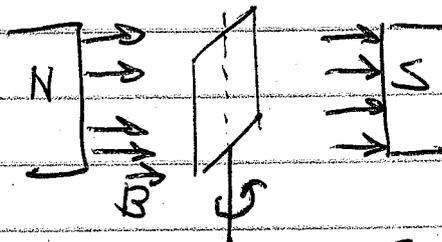
How can we generate voltage?

- Change  $A = \text{Area}$ . Ex: Bar on rails
- Change  $B = \text{magnetic field}$



$$\mathcal{E}_{\text{max}} = \frac{\Delta B}{\Delta t} N A \cos \theta$$

- Change  $\theta = \text{angle}$

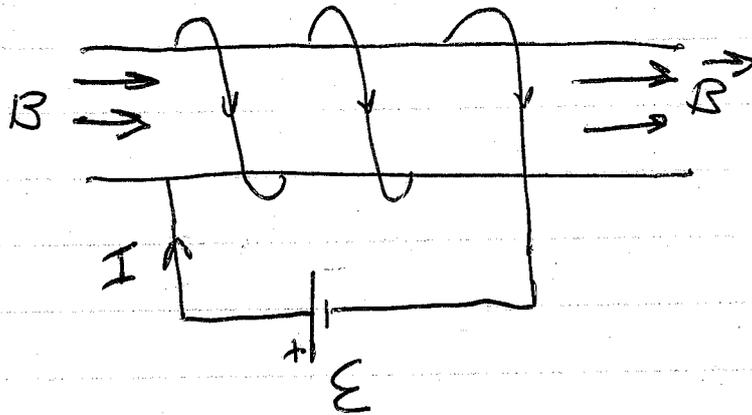


$$\mathcal{E}_{\text{max}} = NBA \omega$$

$\frac{\Delta \theta}{\Delta t}$   $\nearrow$

②

## Solenoid Coil



- Current causes magnetic field

$$B = \frac{\mu_0 N I}{l} = \mu_0 n I$$

$N = \# \text{ loops}$   
 $l = \text{length}$   
 $n = \# \text{ loops/length}$

- Magnetic Field is "Felt" as Flux

$$\Phi_B = N B A \cos \theta$$

$$= N \left( \frac{\mu_0 N I}{l} \right) A$$

$A = \text{area} = \pi r^2$   
 or  $A = w \cdot h$

$$= \underbrace{\left( \frac{\mu_0 N^2 A}{l} \right)}_{\text{constant}} \cdot \underbrace{I}_{\text{variable}} = L \cdot I$$

↑ Inductance

- Changing Flux generates EMF

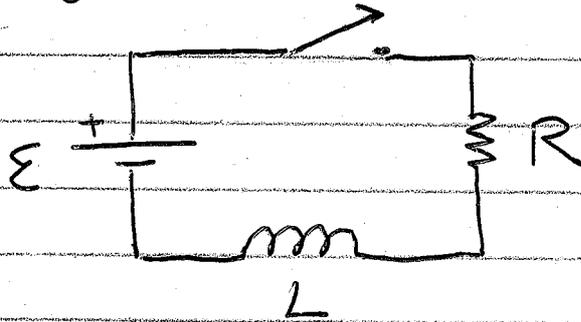
$$\mathcal{E} = - \frac{\Delta \Phi_B}{\Delta t} = - \left( \frac{\mu_0 N^2 A}{l} \right) \frac{\Delta I}{\Delta t} = -L \frac{\Delta I}{\Delta t}$$

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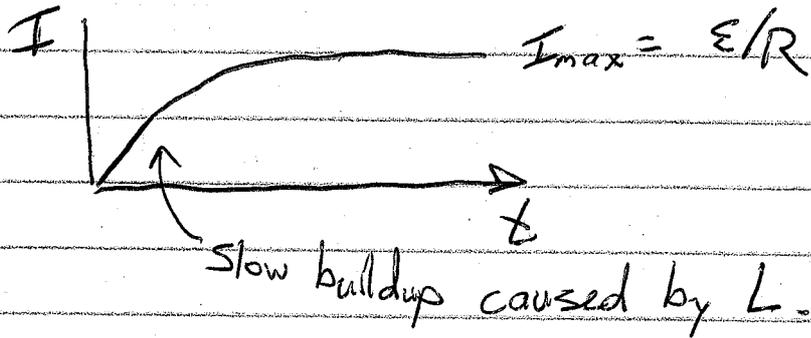
What is inductance (L)?

- Tendency to fight change in current.

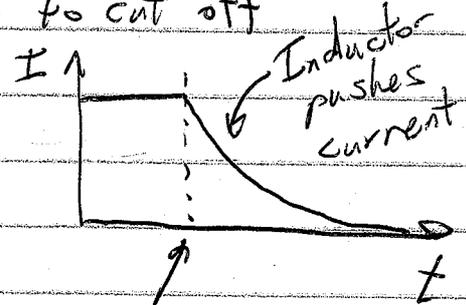
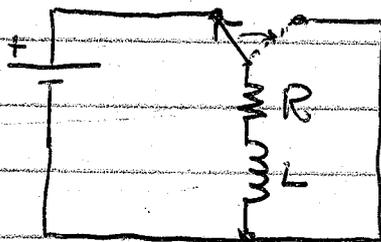
- Current starts @ zero, inductor fights increase in current.



Close switch & current rises slowly.



- Current starts high - try to cut off



"Inductive Kick"

Flip Switch

④

Inductance ( $L$ ) is measured in henries (H).

- Links Flux & Current

$$\Phi_B = L I$$

- Links EMF & Change of Current

$$\mathcal{E} = -L \frac{dI}{dt}$$

Typical Calculation

$$B = \frac{\mu_0 N I}{l} \quad \Phi_B = NBA \quad L = \frac{\Phi_B}{I}$$

Solenoid:  $L = \frac{\mu_0 N^2 A}{l}$

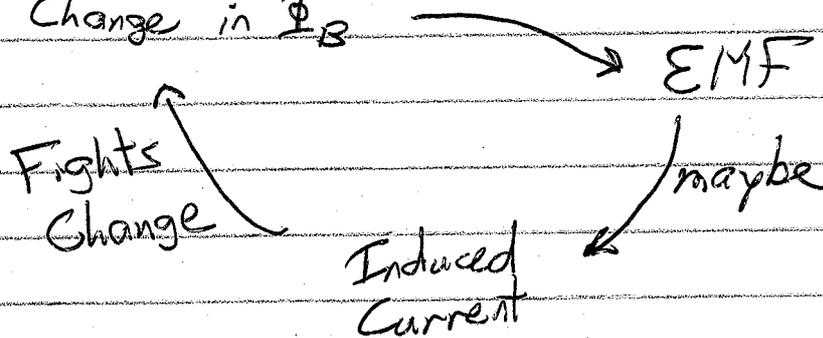
Later: Current will oscillate

- Fast oscillations are fought by inductors.  
Inductor impedes high-frequencies.
- Slow oscillations are fought less
- Zero oscillations are DC and pass without impedance.

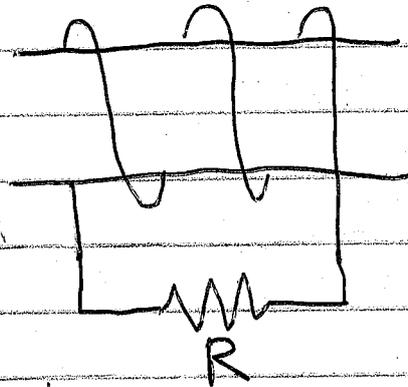
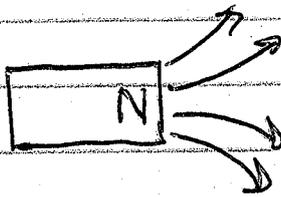
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## Lenz's Law - Direction of EMF

• Change in  $\Phi_B$

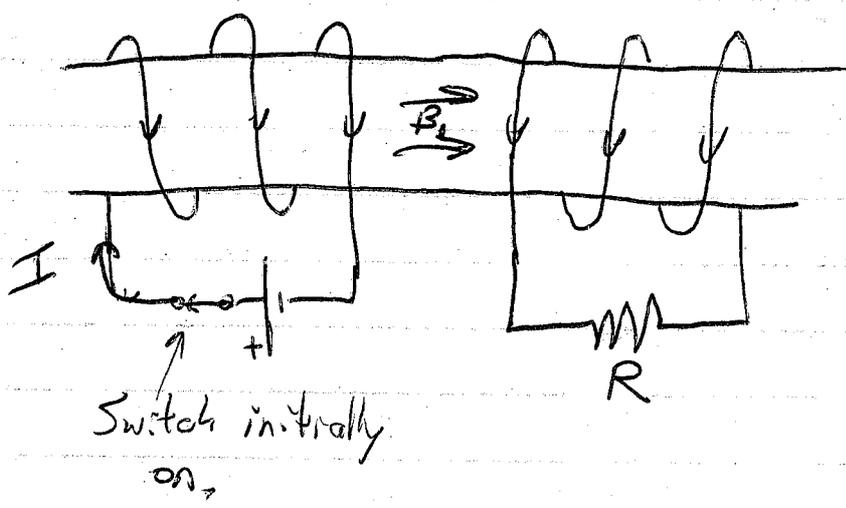


## Solenoid Coil



- ① Bring magnet near coil.
- ②  $\vec{B}$  points right and increasing.
- ③ To Fight the increase, coil makes induced  $B$ :  
 $\vec{B}_{ind} = \underline{\text{left}}$  (to fight increase)
- ④ To generate  $\vec{B} = \text{left}$ , current flows up front, down back in coil.
- ⑤ In the resistor, the current flows to the right.

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- ① Turn switch off, what happens in  $R$ ?
- ②  $B_1$  points to right and is decreasing.
- ③ To fight the decrease,  $B_2 =$  rightward.
- ④ For  $B_2 =$  right,  $I_2 =$  down the front.
- ⑤ In the resistor,  $I_2 =$  Rightward.

