

① Phys 1402 2016-11-10 Lec 23

Doppler Effect - only way to change frequency of coupled oscillations.

As a car drives by hitting the horn:

① High-pitch, getting louder

↑ not doppler
↓ doppler-shifted

② Pitch-change, loud sound

③ Low-pitch, getting quieter

↑

↑
Loudness depends on distance

Doppler-shift of pitch depends on motion

2)

$$\frac{\Delta f}{f} = \frac{v_{rel}}{v_{wave}}$$

$$\frac{192 \text{ Hz}}{4705 \text{ Hz}} = \frac{v_{rel}}{340 \text{ m/s}}$$

$$v_{rel} = 13.9 \text{ m/s} \\ = 31 \text{ MPH}$$

This works for "slow" motion. $\frac{v_{rel}}{v_{wave}} \ll 0.1$

Doppler Radar - The doppler shift happens twice!

$$\frac{\Delta f}{f} = 2 \frac{v_{rel}}{v_{wave}}$$

Ex: Police Radar at 5 GHz

Car driving away @ 30 m/s.

$$\frac{\Delta f}{(5 \times 10^9 \text{ Hz})} = \frac{2 \cdot 30 \text{ m/s}}{3 \times 10^8 \text{ m/s}}$$

$$\Delta f = 1000 \text{ Hz}$$

If "toward"

$$f_{obs} = 5,000,001,000 \text{ Hz}$$

$$\text{Here: } f_{obs} = 4,999,999,000 \text{ Hz}$$

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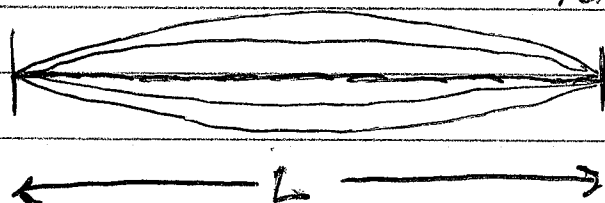
Standing Waves

Lowest Freq:

$$L = \frac{\lambda_1}{2}$$

$$v = f\lambda$$

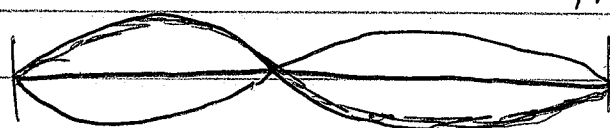
$$f_1 = \frac{v}{\lambda_1} = \frac{v}{2L}$$



Next Freq:

$$L = \lambda_2$$

$$f_2 = \frac{v}{\lambda_2} = \frac{v}{L}$$



Next harmonic:

$$\frac{2}{3}L = \lambda_3$$

$$f_3 = \frac{v}{\lambda_3} = \frac{3v}{2L}$$



$$\text{General: } f_n = n \left(\frac{v}{2L} \right) = n f_1$$

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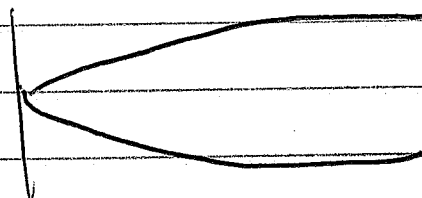
Standing Waves w/ different ends

One side is "node", other is "peak"

$$L = \frac{\lambda_1}{4}$$

$$\lambda_1 = 4L$$

$$f_1 = \frac{v}{\lambda_1} = \frac{v}{4L}$$

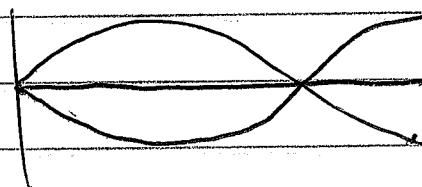


Next Harmonic =

$$L = \lambda \frac{3}{4}$$

$$\lambda = \frac{4L}{3}$$

$$f = \frac{v}{\lambda} = 3 \frac{v}{4L} = 3f_1$$



Different Ends = Odd Harmonics