

What are decibels (dB)?

Relative scale of Energy, Power, Intensity,
Loudness, Brightness, Signal Strength.

Energy is often streamed over time

This is measured as Power:

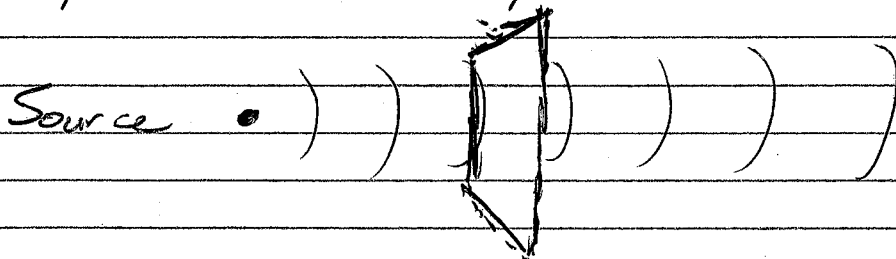
$$P = \frac{\Delta \text{Energy}}{\Delta t}$$

Ex: $1 \text{ W} = 1 \text{ J} / 1 \text{ s}$

$$\text{Energy} = P \Delta t$$

Ex: $1 \text{ kWh} = (1 \text{ kW})(1 \text{ hour})$
 $= (1000 \text{ J/s})(3600 \text{ s})$
 $= 3.6 \text{ MJ}$

Waves spread out in space also.



↳ "catcher" to grab
and measure waves.

Since Power scales w/ size of receiver

$$P = I A$$

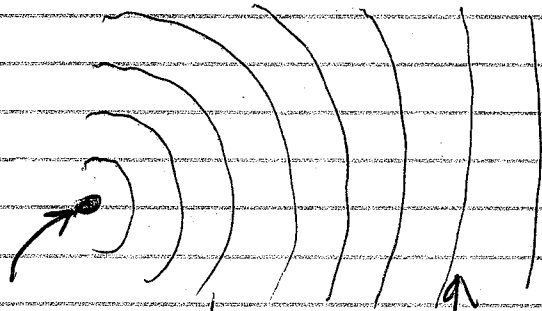
↑ Intensity
↳ Area of receiver

Intensity is

$$I = \frac{P}{A}$$

②

The most spread-out wave is a spherical wave from a point source.



Source generates Power

Wave intensity decreases with distance.

$$P = IA = I(4\pi R^2)$$

Use sphere because all points receive the same intensity of waves.

$$I = \frac{P}{4\pi R^2} \quad (\text{Point Source})$$

These units have a huge Dynamic Range

$$\text{Dynamic Range} = \frac{\text{Strongest Energy}}{\text{Weakest Energy}}$$

$$\text{Ex: Hearing} \quad \frac{1 \text{ W/m}^2}{10^{-12} \text{ W/m}^2} = 10^{12}$$

Our perception scales with the power of 10.
This is a logarithmic scale.

$$\text{Ex: } I = 3 \times 10^{-5} \text{ W/m}^2$$

Power of 10 is -5
Minor adjustment is 3x

③

decibels provide a number system where the power of 10 comes first, then the minor adjustment.

$$3 \times 10^{-5} = 10^x \quad \text{for some } x.$$

$$10^{-5} = 1 \times 10^{-5} \quad \text{Too small}$$

$$10^{-4} = 10 \times 10^{-5} \quad \text{Too big}$$

$$10^{-4.5} = 3.16 \times 10^{-5} \quad \text{Very close}$$

$$10^{-4.4} = 3.98 \times 10^{-5} \quad \text{Even worse}$$

$$10^{-4.6} = 2.5 \times 10^{-5} \quad \text{Too small}$$

$$10^{-4.52} = 3.02 \times 10^{-5} \quad \text{Closest w/ 2 decimal}$$

To interpret as decibels, just use the power of 10.

$$3 \times 10^{-5} \rightarrow \begin{aligned} & -4.52 \text{ bels} \\ & -45.2 \text{ decibels} \\ & \approx -45 \text{ dB} \end{aligned}$$

$$\text{Easy way: } \log(3 \times 10^{-5}) = -4.52$$

$$10 \log(3 \times 10^{-5}) = -45.2$$

$$\text{To turn a number } (x) \text{ into dB: } 10 \log(x)$$

What do we use as x ?

Every quantity is a scaling factor of a unit.

dB measurements are always relative to some reference quantity.
 ↑ numerical part is x .

The dB level corresponds to a scaling factor.

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level (dB)

Factor

10 dB

$$10^{1.0} = 10$$

20 dB

$$10^{2.0} = 100$$

30 dB

$$10^{3.0} \approx 1000$$

1 dB

$$10^{0.1} = 1.258 \approx 26\% \text{ increase}$$

3 dB

$$10^{0.3} = 2$$

6 dB

$$10^{0.6} = 4$$

9 dB

$$10^{0.9} = 8$$

Increase by adding 3 dB

Increase by doubling

(*)

As energy scales by multiplication, decibel levels increase by addition.

0 dB

$$10^0 = 1$$

Zero dB is not nothing, it is a factor of one. 0 dB means no change from the reference.

-3 dB

$$10^{-0.3} = 0.5$$

(Decrease by factor of 2)

~~3x10~~
 $+5 \text{ dB} - 50 \text{ dB} = -45 \text{ dB}$

$$3 \times 10^{-5}$$

$$10 \log 3 = 10(0.5) = 5$$
$$10 \log(10^{-5}) = 10(-5) = -50$$

$$3 \text{ dB} \rightarrow 2$$

$$5 \text{ dB} \rightarrow 3$$

$$7 \text{ dB} \rightarrow 5$$

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What does 86 dB mean?

$$\begin{array}{l}
 10 \text{ dB} \\
 + 10 \text{ dB} \\
 \vdots \\
 + 3 \text{ dB} \\
 + 3 \text{ dB}
 \end{array}
 \left. \vphantom{\begin{array}{l} 10 \text{ dB} \\ + 10 \text{ dB} \\ \vdots \\ + 3 \text{ dB} \\ + 3 \text{ dB} \end{array}} \right\} 8 \text{ times}$$

$$\begin{array}{l}
 10 \\
 \times 10 \\
 \vdots \\
 \times 2 \\
 \times 2
 \end{array}
 \left. \vphantom{\begin{array}{l} 10 \\ \times 10 \\ \vdots \\ \times 2 \\ \times 2 \end{array}} \right\} 8 \text{ multiplications}$$

$$\begin{aligned}
 &= 2 \cdot 2 \cdot 10^8 \\
 &= 4 \times 10^8
 \end{aligned}$$

What reference levels are used?

Sound: Quietest Audible sound $I_0 = 10^{-12} \text{ W/m}^2$

Typical conversation $\sim 70 \text{ dB}$

What intensity is this?

$$\text{Scaling Factor} = 10^7$$

$$I = (10^7) (10^{-12} \text{ W/m}^2) = 10^{-5} \text{ W/m}^2$$

Dynamic Range

$$\text{Ratio} = \frac{I_{\max}}{I_{\min}} \quad \text{or} \quad \frac{P_{\max}}{P_{\min}}$$

Vision: 90 dB

LCD TV: 1000:1

$$10 \log(1000) = 30 \text{ dB}$$

Hearing: 120 dB

CD: 16-bit voltage

$$\frac{2^{16}}{2^0} = 65536 \text{ Voltage Ratio}$$

$$90 \text{ dB} + 6 \text{ dB} = 96 \text{ dB}$$

$$P = I V = \frac{V}{R} V = \frac{V^2}{R}$$

$$\text{Power Ratio} = 65536^2 = 4.3 \times 10^9$$