

① Phys 1402

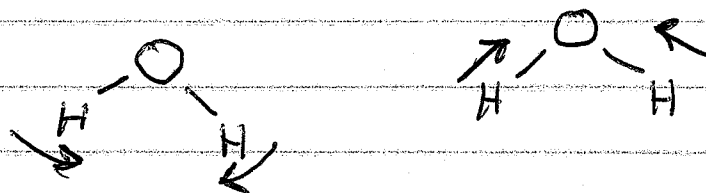
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Lec 12

- Oscillations
- repetitive behavior
  - Equilibrium where the value can be naturally constant.
  - Restoring force - tendency back toward equilibrium.
  - Inertia - overshoots equilib.

Examples:

- Mass on a spring
- Vibrating diving board
- Pendulum
- Molecules



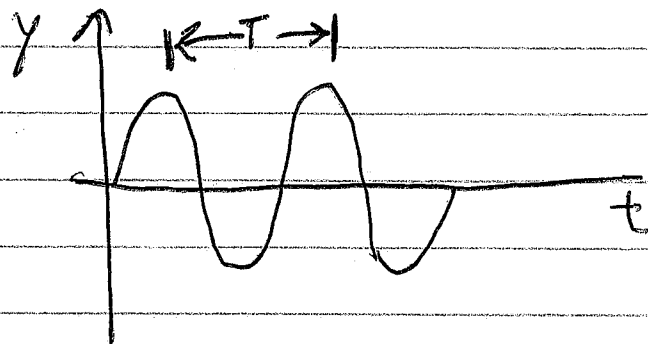
- Nuclei in magnetic fields (NMR, MRI)
- AC Voltage, Current
- Pieces of waves

②

## Language of oscillations

Vertical on the graph:

- Displacement
- Equilibrium
- Amplitude -  
max displacement
- Energy - proportional to amplitude squared.



Horizontal axis: Timing

- Period ( $T$ ) - time of repetition.
- Frequency ( $f$ ) -  $f = 1/T$  # repetitions per unit time.

Generic equation:  $y = y_0 \sin(2\pi f t + \phi)$

$y_0$  = amplitude

$f$  = frequency

$\phi$  = phi = phase shift

Does this repeat every  $T$ ?

$\sin()$  repeats every  $2\pi$

start @  $t=0$

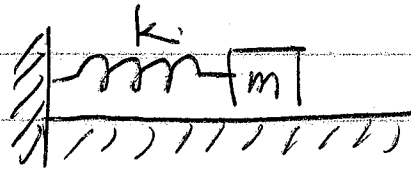
$$2\pi f t = 0$$

cycle?  $t=T$

$$2\pi f T = 2\pi \left(\frac{1}{T}\right) T = 2\pi \checkmark$$

3

## Simple Harmonic Oscillator - mass & spring



no friction

$m =$  mass

$k =$  spring constant  
or stiffness

Force  $F = -kx$   
Newton's 2<sup>nd</sup>

Law:  $F = ma$

When  $x$  is  $\oplus$  accel is  $\ominus$

$x = 0$  accel is  $0$

$x$  is  $\ominus$  accel is  $\oplus$

Frequency:  $f = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$

Stiffer  $\Rightarrow$  faster oscillation

more mass  $\Rightarrow$  slower

Ex: Car suspension

$m = 2000$  kg

$f = 2$  Hz

$$\begin{aligned} k &= m(2\pi f)^2 \\ &= (2000)(2\pi(2))^2 \\ &= 316,000 \text{ N/m} \end{aligned}$$

$$\begin{aligned} 2\pi f &= \sqrt{k/m} \\ (2\pi f)^2 &= k/m \end{aligned}$$

$\times$  when  $F =$  weight of car  
 $F = mg = (2000)(9.8)$   
 $= 19600$  N

(A)

Check  $|F| = kx$

$$(19600 \text{ N}) = (316000 \text{ N/m}) x$$

$$0.06 \text{ m} = x$$

6 cm = spring compression

Pendulum

$$f = \frac{1}{2\pi} \sqrt{\frac{g}{L}}$$

← prop to restoring force  
← prop to "inertia"