

① Phys 2426 2014-11-19

Index of Refraction

I told you: $v_{\text{light}} = c = 3 \times 10^8 \text{ m/s}$

Actually, $v_{\text{light}} = c$ only in a vacuum

Materials slow light by a factor of n .

$$n = \text{index of refraction} \quad v = \frac{c}{n}$$

As light changes materials, $f = \text{const.}$

$$v = f\lambda \quad \lambda_n = \frac{\lambda_0}{n}$$

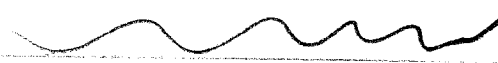
Every n is > 1 . Generally $1 < n < 5$

$$\text{Ex: } n_{\text{air}} = 1.003$$

$$n_{\text{water}} = 1.33$$

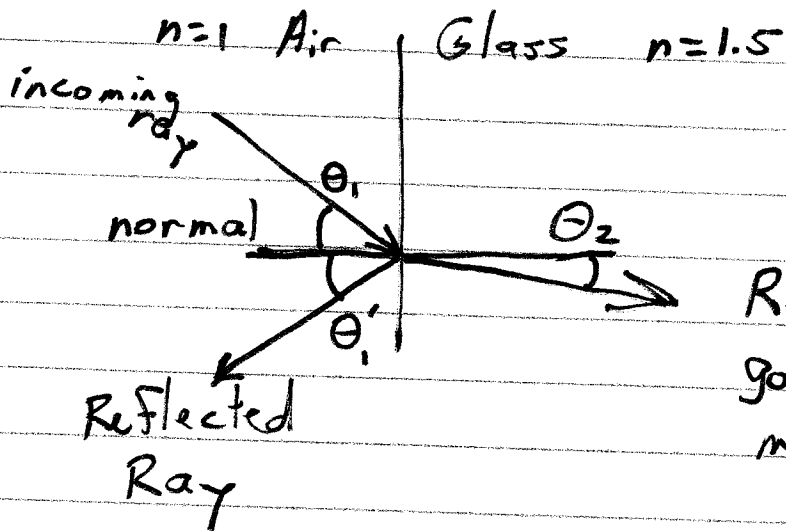
$$n_{\text{glass}} = 1.5$$

Ex: Speed of light under water

$$v = \frac{c}{n} = \frac{3 \times 10^8 \text{ m/s}}{1.33} = 2.26 \times 10^8 \text{ m/s}$$


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Reflection & Refraction



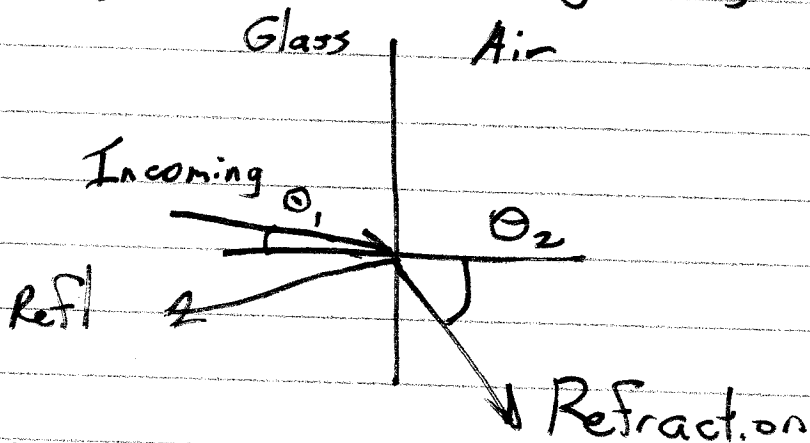
Refracted ray goes into new material.

$$\theta_1 = \theta_1'$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

If n increases, $\sin \theta$ decr.

When light leaves the glass, it speeds up.



Note: $\sin \theta_2$ is limited to 1

Set $\sin \theta_2 = 1$ to find largest θ_1 .

$$n_1 \sin \theta_1 = n_2$$

$$\sin \theta_1 = n_2 / n_1 \quad \text{"critical angle"}$$

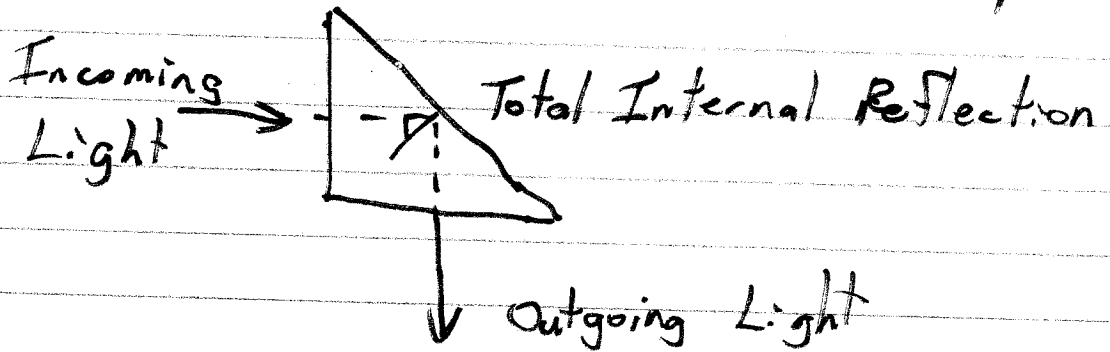
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Total Internal Reflection: θ_2 not allowed.

To have this, n_1 must be larger (than n_2).

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\sin \theta_2 = \frac{n_1}{n_2} \sin \theta_1$$



$$\theta_1 = 45^\circ$$

$$n_2 = 1$$

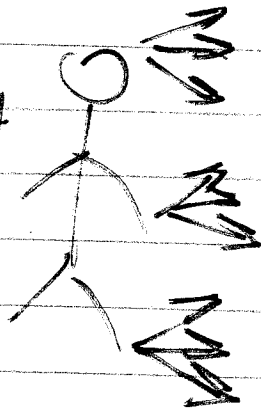
$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$n_1 \sin 45^\circ = (1)(1)$$

$$n_1 = 1.414 \text{ at a minimum}$$

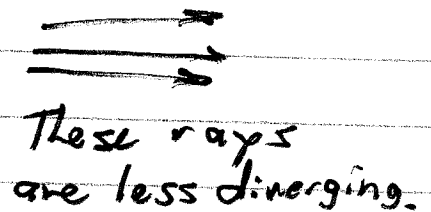
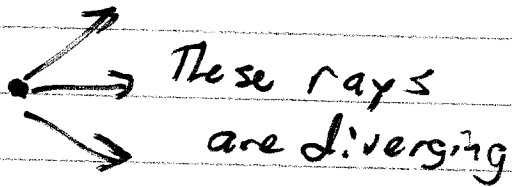
Image Formation

Every part
of the object
Emits light
in all
directions.



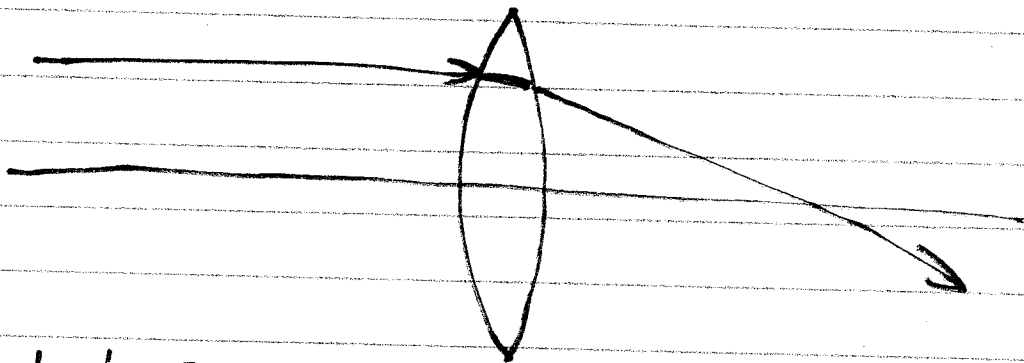
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We will consider a point source.



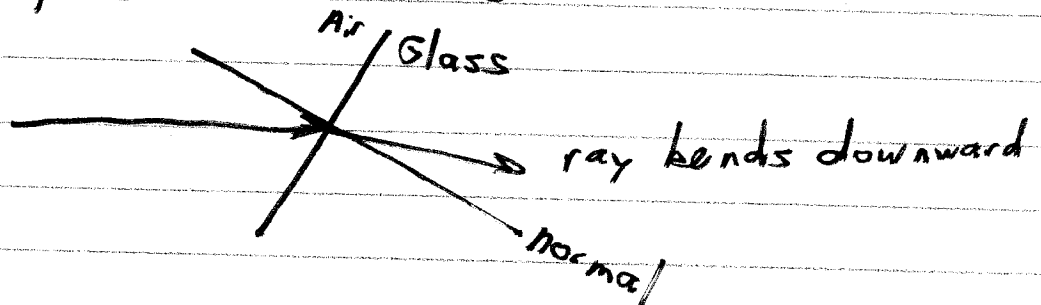
Everything we see causes diverging rays.
We control the divergence of rays to control the appearance.

Converging Lens: Thicker in the middle.

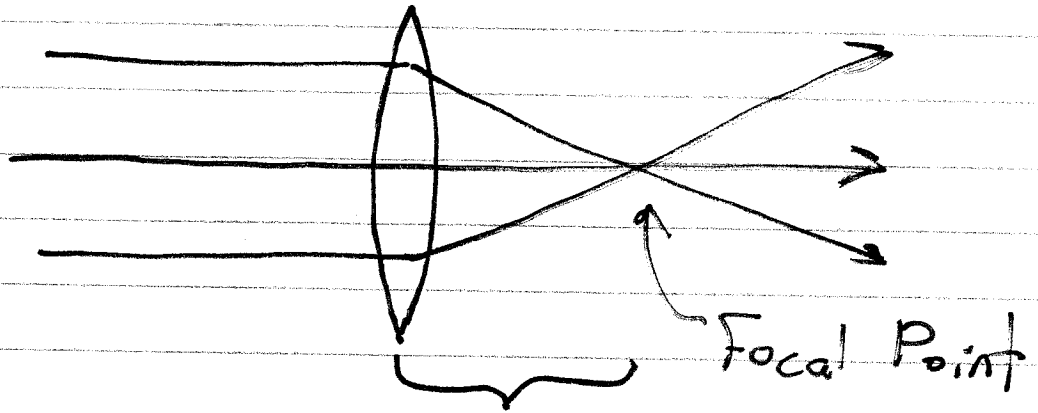
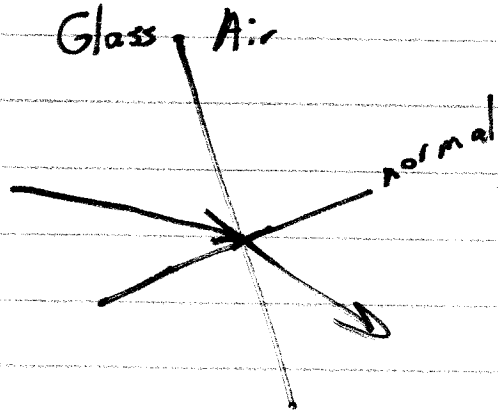


Central Ray: $\theta_1 = 0 \Rightarrow \theta_2 = 0$

Upper Ray @ Front surface

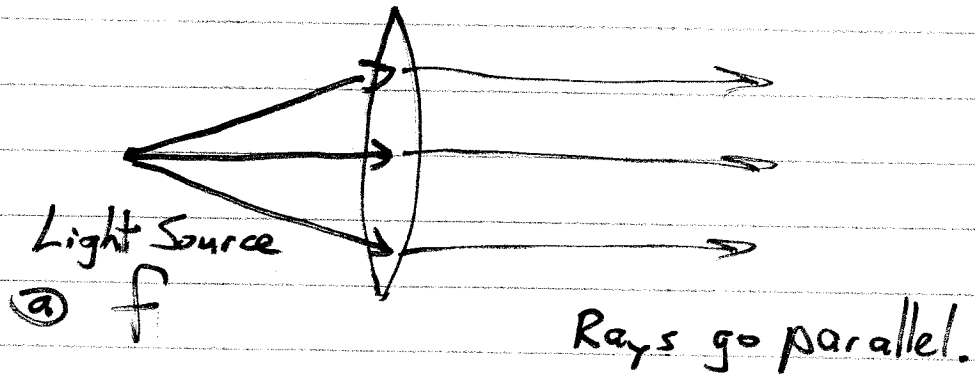


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Focal Distance
Parallel Rays are focused @ Focal Distance.

The rays can be reversed.



3 Important Rays

1. Central Ray goes straight thru middle of lens.
2. Incoming Parallel Ray bends to line up w/ focal point.
3. Focal Ray bends parallel to axis.

Measurements w/ Lenses - Distance to the current lens is the important quantity.

p - object distance

q - image distance

$$\frac{1}{p} + \frac{1}{q} = \frac{1}{f}$$

Note: If $\frac{1}{q} = 0$, the behavior "flips".
 $p = f$ is a critical point.