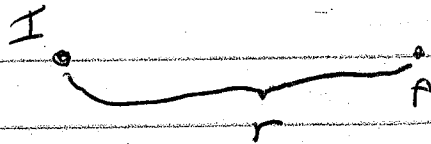
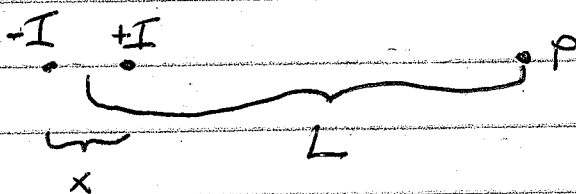


B of a single wire



$$B = \frac{\mu_0 I}{2\pi} \frac{1}{r}$$

B of a pair of wires



$$B = \frac{\mu_0 I}{2\pi(L + \frac{x}{2})} - \frac{\mu_0 I}{2\pi(L - \frac{x}{2})}$$

• Known L - just plug in values

• Known B - L is unknown; must solve

$$B = \left( \frac{\mu_0 I}{2\pi} \right) \left[ \frac{1}{L + \frac{x}{2}} - \frac{1}{L - \frac{x}{2}} \right]$$

Distance

B

37 cm

17.5 nT

117 cm

1.75 nT

3.2 times more

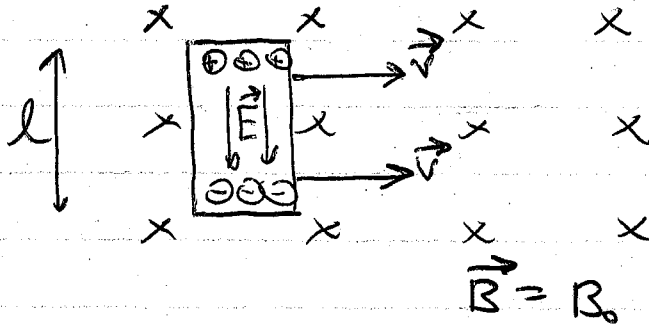
10 times less

$\sqrt{10}$  times more

②

## Motional EMF

Thought process:



①  $\vec{F}_B = qvB$  (up)

② Charges cause  $\vec{E} = E_0$  (down)

③ Charges feel no force when

$$F_E = F_B \quad (\text{magnitudes})$$

$$qE_0 = qvB_0$$

$$E_0 = vB_0$$

④ Electric field is negative gradient of voltage  
 negative  $\swarrow$   $\searrow$  slope or derivative

$$\Delta V = \text{"EMF"} = \mathcal{E} = E l$$

$$\mathcal{E} = v B l$$

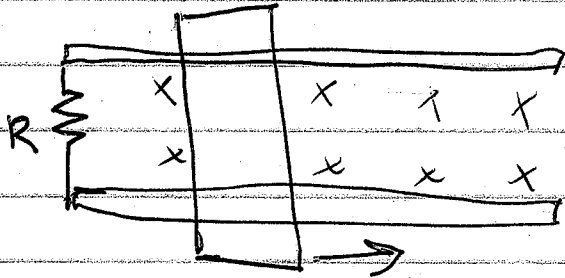
③

How can we use this voltage in a circuit?

Method 1: Hook wires to it, Attach Load to the moving metal.

Problem: The wires generate the opposite voltage. Can't even measure w/ voltmeter on plane.

Method 2: Mount the bar on rails



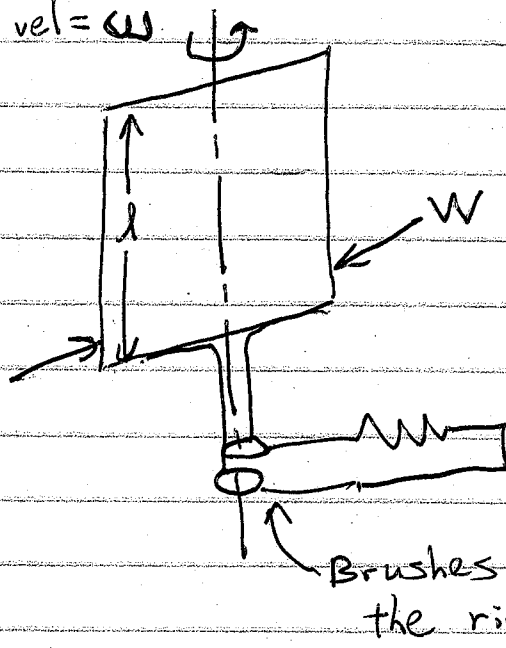
Bar moves, circuit doesn't. Used in the shake light. Inconvenient, but straightforward.

$$\begin{aligned} \mathcal{E} &= vBl \\ \mathcal{E} &= V \\ V &= IR \end{aligned}$$

Method 3: Mount the bar on a rotating frame.

Angular vel =  $\omega$

$$v = \omega R$$



$$\begin{aligned} \mathcal{E} &= Bl\omega R \\ &= BA\omega \quad \leftarrow \text{loop} \end{aligned}$$

$$\mathcal{E} = NBA \omega \quad \leftarrow \text{coil}$$

$$\text{Recall: } \tau = NBA I$$

(4)

Similar result for Watt Balance

The given EMF was the "peak" or amplitude of a varying  $\mathcal{E}$ .

$$\mathcal{E}(t) = \mathcal{E}_0 \cos(\omega t)$$

↑  
NBA  $\omega$

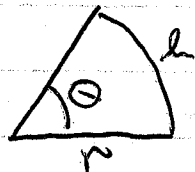
Angular Speed is measured in radians per second.

$$\text{Ex: } 3600 \text{ RPM} = 3600 \left( \frac{2\pi \text{ rad}}{60 \text{ s}} \right)$$

$$1 \text{ rotation} = 2\pi \text{ rad}$$

$$3600 \text{ RPM} = 377 \text{ rad/s} = 377 \text{ s}^{-1}$$

Note: radian is dimensionless



$$l = r\theta$$

$$\frac{l}{r} = \theta$$

Ex: Full circumference

$$\theta = \frac{2\pi r}{r} = 2\pi$$

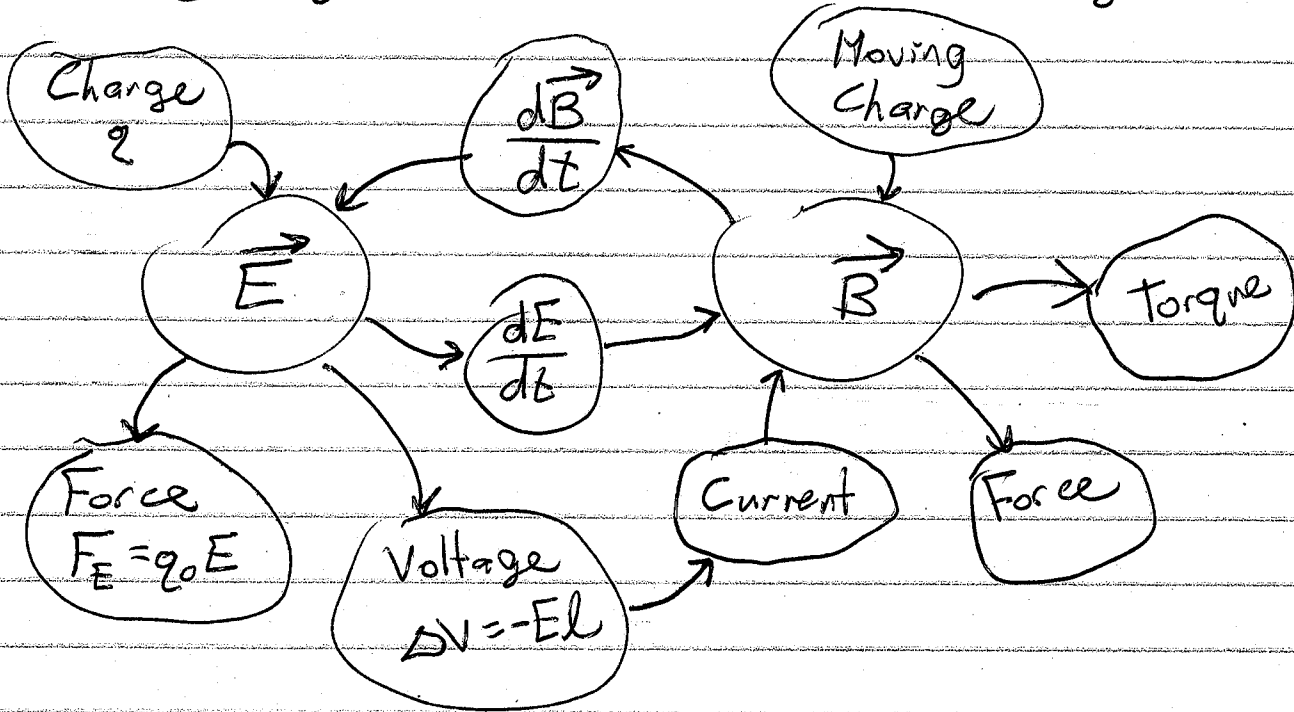
=  $2\pi$  radians

5

It doesn't matter if the coil  
or the magnet moves.

Moving Coil  $\Rightarrow$  Motional EMF  $\Rightarrow$  Voltage

Moving Magnet  $\Rightarrow$  ?  $\Rightarrow$  Voltage



Faraday's Law

$$\mathcal{E} = - \frac{d\Phi_B}{dt}$$

Magnetic Flux

$$\Phi_B = N B A \cos \theta$$