1. What is the symbol for impedance?
$>Z$
2. What is the unit of inductance?
$>$ henries, H
3. In the image to the right, the magnetic field is caused by a current in the wire that stretches across the middle of the diagram. What is the direction of the current in the wire?
$>$ Toward the left
4. A wire is carrying a current that flows horizontally northward. If you want to levitate the wire with magnetism, in what direction should the magnetic force point?
> The magnetic force should point up (toward the sky, out of the page on a map).
5. A wire is carrying a current that flows horizontally northward. If you want to levitate the wire with magnetism, in what direction should the magnetic field point?

| $\times$ | $\times$ | $\times$ | $\times$ |
| :--- | :--- | :--- | :--- |
| $\times$ | $\times$ | $\times$ | $\times \overrightarrow{\mathbf{B}}_{\text {in }}$ |
| $\times$ | $\times$ | $\times$ | $\times$ |
|  | $\bullet$ | $\bullet$ | $\bullet$ |
| $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
|  | $\cdot$ | $\overrightarrow{\mathbf{B}}_{\text {out }}$ |  |

$>$ The magnetic field should point West (left on a map).
6. When looking along the axis of a coil, it is producing a magnetic field that is pointing away from you. In what direction is the current in the coil?
> Clockwise
7. A solenoid like the "outer coil" in our laboratory has 3000 turns of wire spread out over the 10 cm length. The wire is wrapped around a plastic core with a radius of 2 cm . If the current in the coil is 2 A , what is the magnetic field?
$>B=\frac{\mu_{0} N I}{\ell}=\frac{\mu_{0}(3000)(2 \mathrm{~A})}{0.1 \mathrm{~m}}=0.0754 \mathrm{~T}=75.4 \mathrm{mT}$
8. In the diagram to the right, two wires are carrying currents in opposite directions. Where is there a location in which the total magnetic field is zero?

a. Region I only
b. Region II only
c. Region III only
d. Region I or II
e. Any of the 3 regions.
$>$ In Region II, both currents produce magnetic fields into the page, so it can't possibly be there.
> To add to zero, the two contributions must be equal in magnitude, so the point must be closer to the weaker current. Therefore, the point can't be in Region I.
9. A proton enters a region of uniform magnetic field with a velocity of $\vec{v}=5 \times 10^{6} \mathrm{~m} / \mathrm{s}$ in the $+\hat{y}$ direction. The magnetic field has a magnitude of 3.0 T and points in the $-\hat{z}$ direction. What is the magnetic force exerted on the proton?
$\Rightarrow$ Magnitude: $F_{B}=q v_{\perp} B=\left(1.6 \times 10^{-19}\right)\left(5 \times 10^{6}\right)(3.0)=2.4 \times 10^{-12} \mathrm{~N}$
$>$ Direction: Leftward, $-\hat{x}$
10. In the mass spectrometer shown to the right, the electric field has a magnitude of $2000 \mathrm{~V} / \mathrm{m}$ and the magnetic field (in both parts) has a magnitude of 0.005 T . What is the speed of the particles that get through the velocity selector?
$>$ The electric and magnetic forces must be equal and opposite. $q E=q v B$, so (2000) $=v(0.005)$ and $v=400,000 \mathrm{~m} / \mathrm{s}$.
11. In the mass spectrometer in the previous question, what is the radius of the path of protons in the mass spectrometer region?
$>$ In a mass spec, the radius is $r=\frac{m v}{q B}=\frac{\left(1.67 \times 10^{-27}\right)(400,000)}{\left(1.6 \times 10^{-19}\right)(0.005)}=0.835 \mathrm{~m}$

12. The diagram to the right models a coaxial cable. In the center, $I_{1}=3.0 \mathrm{~A}$ is flowing out of the page. Surrounding it is a thin shell of radius $2 d$ carrying a current $I_{2}=3.0 \mathrm{~A}$ into the page. If $d=0.02 \mathrm{~m}$, what is the magnetic field at point $b$ ?
$>$ At point $b$, draw a loop around the entire wire.

$$
\oint \vec{B} \cdot d \vec{l}=2 \pi r B=2 \pi(3 d) B
$$

$>$ Inside that loop, both $I_{1}$ and $I_{2}$ contribute to the enclosed current.

$$
I_{e n c}=(3.0 \mathrm{~A})+(-3.0 \mathrm{~A})=0.0 \mathrm{~A}
$$


> By Ampere's Law, the magnetic field is zero.

$$
\begin{gathered}
\oint \vec{B} \cdot d \vec{l}=\mu_{0} I_{e n c}=0 \\
B=0
\end{gathered}
$$

13. If a magnetic field and an electric field are pointing in opposite directions, how can the net force (electric plus magnetic) on an electron be equal to zero?
a. If the electron is stationary.
b. If the electron is moving in the direction of the electric field vector.
c. If the electron is moving in the direction of the magnetic field vector.
d. If the electron is moving perpendicular to the electric field vector.
e. It is not possible for the net force to be zero.
$>$ The magnetic force must be perpendicular to $\vec{B}$, so it can't cancel the electric force.
14. A rectangular loop with mass 0.6 kg is 2.0 m wide and 3.0 m high. It is dropped so that the bottom leg of the loop is in a magnetic field $B_{\text {in }}=6.0 \mathrm{~T}$, while the top leg is out of the magnetic field. If the resistance of the loop is $40 \Omega$, at what speed does it fall with zero acceleration?
> The force on the bottom segment must offset gravity:

$$
F_{g}=m g=(0.6 \mathrm{~kg})(9.8 \mathrm{~N} / \mathrm{kg})=5.88 \mathrm{~N}
$$

$>$ This magnetic force determines the current:

$$
\begin{aligned}
& F=I \ell B \\
& I=\frac{F}{\ell B}=\frac{5.88 \mathrm{~N}}{(2.0 \mathrm{~m})(6.0 \mathrm{~T})}=0.49 \mathrm{~A}
\end{aligned}
$$


> The EMF in the loop is:

$$
\varepsilon=I R=(0.49 \mathrm{~A})(40 \Omega)=19.6 \mathrm{~V}
$$

$>$ The EMF determines the velocity:

$$
\begin{aligned}
\varepsilon & =v B \ell \\
v & =\frac{\varepsilon}{B \ell}=\frac{19.6 \mathrm{~V}}{(6.0 \mathrm{~T})(2.0 \mathrm{~m})}=1.63 \mathrm{~m} / \mathrm{s}
\end{aligned}
$$

15. In the previous question, when the loop is in the position shown, in what direction does the current flow in the loop?
a. Clockwise
b. Counter-clockwise
c. Up
d. Down
e. Inward
$>$ In the bottom segment of the loop, $\vec{v}$ is toward the bottom of the page, $\vec{B}$ is into the page, so the force is the right. This pushes $\oplus$ charges rightward in the bottom segment, and they bend CCW to follow the loop.
16. A coil is wrapped with 300 turns of wire on the perimeter of a square frame (side length $=20 \mathrm{~cm}$ ). Each turn has the same area as the frame, and the total resistance of the coil is $1.5 \Omega$. A uniform magnetic field perpendicular to the plane of the coil changes in magnitude at a constant rate from 0.50 T to 0.90 T in 2.0 s . What is the magnitude of the induced emf in the coil while the field is changing?
$>\varepsilon=N A \frac{\Delta B}{\Delta t}=(300)(0.2)^{2}\left(\frac{0.9-0.5}{2.0}\right)=2.4 \mathrm{~V}$
17. A current may be induced in a coil by
a. moving one end of a bar magnet through the coil.
b. moving the coil toward one end of the bar magnet.
c. holding the coil near a second coil while the electric current in the second coil is increasing.
d. all of the above.
e. none of the above.
18. An 8 mH inductor is modified by unwinding half of the loops of wire (without changing the radius or length of the inductor). What is the new inductance of the inductor?
$>$ The magnetic field is proportional to $N$, and the magnetic flux is $\Phi_{B}=N B A$, which brings in another factor of $N$. This makes the inductance proportional to $N^{2}$. Halving the number of loops would reduce the inductance to 2 mH .
19. An AC generator consists of 6 turns of wire. Each turn has an area of $0.040 \mathrm{~m}^{2}$. The loop rotates in a uniform field $(\mathrm{B}=0.20 \mathrm{~T})$ at a constant angular frequency of $314 \mathrm{rad} / \mathrm{s}$. What is the maximum induced emf?
$\Rightarrow \varepsilon_{\max }=N B A \omega=(6)(0.20)(0.040)(314)=15 \mathrm{~V}$
20. What is the average power used by a $10 \Omega$ resistor when supplied by $V_{R M S}=12 \mathrm{~V}$ at a frequency of 1000 Hz ?
$>I_{R M S}=\frac{V_{R M S}}{R}=\frac{12 \mathrm{~V}}{10 \Omega}=1.2 \mathrm{~A}$, then $P_{\text {avg }}=V_{R M S} I_{R M S}=(12 \mathrm{~V})(1.2 \mathrm{~A})=14.4 \mathrm{~W}$
$>$ If this was an inductor or capacitor, $P_{\text {avg }}=0$.
21. A series $R L C$ circuit has a resistance of $26.0 \Omega$ and an impedance of $71.0 \Omega$. What average power is delivered to this circuit when $\Delta V_{\mathrm{rms}}=210 \mathrm{~V}$ ?
$\Rightarrow$ The current is $I_{R M S}=(210 \mathrm{~V}) /(71.0 \Omega)=2.958 \mathrm{~A}$
$>$ The power is used only by the resistor. $P=I V=I^{2} R=(2.958 \mathrm{~A})^{2}(26.0 \Omega)=227 \mathrm{~W}$
22. An AC voltage source is connected across a capacitor, and 4.0 mA of current flows. If the frequency is tripled while keeping the RMS voltage constant, what is the new current through the capacitor?
$>$ For a capacitor, frequency and reactance are inversely proportional, so $X_{C}$ decreases $3 \times$.
$>$ The current and reactance are inversely proportional, so $I$ increases $3 \times$.
23. At what frequency will a 50.0 mH inductor have a reactance $\mathrm{X}_{\mathrm{L}}=700 \Omega$ ?
$>X_{L}=2 \pi f L$, so $f=X_{L} /(2 \pi L)=(700 \Omega) /(2 \pi(0.050 \mathrm{H}))=2230 \mathrm{~Hz}$
24. The inductance of a tuning circuit of an AM radio is 4.00 mH . Find the capacitance of the circuit required for reception at 1200 kHz .
$>X_{L}=X_{C}=2 \pi f L=1 /(2 \pi f C)$, so $C=1 /\left((2 \pi f)^{2} L\right)=4.4 \times 10^{-12} \mathrm{~F}=4.4 \mathrm{pF}$
25. A transformer is plugged into the wall ( $V_{R M S}=120 \mathrm{~V}, f=60 \mathrm{~Hz}$ ) and provides an output of $V_{R M S}=12 \mathrm{~V}$.

If the source is changed to DC 120 V , what will the output voltage be?
$>$ The output voltage is 0 when DC is applied to a transformer.

All of the questions on this page use this circuit formed from a $1 \mathrm{k} \Omega$ resistor, a 1 H inductor, and a $1 \mu \mathrm{~F}$ capacitor. The voltage of the source is $140 \sin (500 t)$.
26. Determine the rms voltage for the signal generator.
$>V_{R M S}=\frac{V_{\max }}{\sqrt{2}}=\frac{140}{\sqrt{2}}=99 \mathrm{~V}$
27. Determine the impedance for the circuit.
$\Rightarrow$ From the sine, $2 \pi f=500($ in rad $/ \mathrm{s})$.
$>$ Inductor: $X_{L}=2 \pi f L=(500)(1.0 \mathrm{H})=500 \Omega$

$\Rightarrow$ Capacitor: $X_{C}=\frac{1}{2 \pi f C}=\frac{1}{(500)\left(1.0 \times 10^{-6} \mathrm{~F}\right)}=2000 \Omega$
$>$ Reactance: $X=X_{L}-X_{C}=-1500 \Omega$
$\Rightarrow$ Impedance: $Z=\sqrt{R^{2}+X^{2}}=\sqrt{1000^{2}+1500^{2}}=1803 \Omega$
28. Determine the resonant frequency of the circuit.
$>f_{R}=\frac{1}{2 \pi \sqrt{L C}}=\frac{1}{2 \pi \sqrt{(1.0)\left(1.0 \times 10^{-6}\right)}}=159 \mathrm{~Hz}$
29. Determine the rms voltage drop across the capacitor in the circuit.
$\Rightarrow V_{C}=I X_{C}=(0.0549 \mathrm{~A})(2000 \Omega)=109.8 \mathrm{~V}$
Weird that it's more than the voltage of the power supply, but true! The inductor generates extra voltage.
30. The primary winding of an electric train transformer has 400 turns and the secondary has 50 . If the input RMS voltage is 120 V what is the output RMS voltage?
$>\frac{V_{S}}{V_{P}}=\frac{N_{S}}{N_{P}}$, so $\frac{V_{S}}{120}=\frac{50}{400}$, and $V_{S}=15 \mathrm{~V}$.

