

t	# cases	$\Delta\#/\Delta t$	$\Delta\#/\#$
1989	23.4	21.1 - 23.4	
< 1	21.1	-2.3	$-2.3/23.4 = -9.8\%$
< 2	18.0	-3.1	$= -14.7\%$
< 3	16.1	-1.9	$= -10.6\%$
< 4	13.4	-2.7	$= -16.8\%$
5	12.5	-.9	$= -6.7\%$
6	10.8	-1.7	$= -15.7\%$

Is a linear model reasonable?

- Slopes constant? / No, jumpy
- graph linear? / Yes, $m \approx -2$
- Yes if line-kind of
- No if curve
- Make sense?

No b/c negative # in ~ 6 yrs

Is an exponential model reasonable?

- Method I - Are % changes ~ constant?
- No % change not constant
- Yes % change varies but ~ -10%

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(2)

What is an exponential model?

$$y = k \cdot a^t$$

k = starting value a = growth factor

(23.4)

= $1 + \text{growth rate}$

→ older % ~~-16.8~~, ~~-15.7~~, -14.7, -10.6, ~~-9.8~~, ~~-6.7~~

$$- .1265 = -12.65\%$$

growth rate

$$a = 1 + (-.1265) = .8735$$

$a < 1 \leftrightarrow$ decay

$a > 1 \leftrightarrow$ growth

$$y = 23.4 \cdot 0.8735^t$$

y = # new cases Hep B

t = yrs since 1989

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(3)

Exponential Models (growth)

have constant doubling times

DT = doubling time

Starting value for $y = k$

Doubled value for $y = \underline{2k}$

At DT

$$\frac{2k}{k} = \frac{k}{k} \cdot a^{DT}$$

Solve $2 = a^{DT}$ for DT

$$\log(2) = \log(a^{DT})$$

$$\log(2) = DT \cdot \log(a)$$

$$\frac{\log(2)}{\log(a)} = DT$$

Knowing "a" we can find DT

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(4)

Example (A) $r = 4\% = .04$

$$Q = 1 + .04 = 1.04$$

$$DT = \frac{\log 2}{\log(1.04)}$$
$$= 17.67 \text{ yrs}$$

(B) US Pop $r \approx 1\%$

$$Q = 1 + .01 = 1.01$$

$$DT = \frac{\log 2}{\log(1.01)} = 69.7 \text{ yrs}$$

$$2 = Q^{DT}$$

$$Q = 2^{1/DT}$$

$$Q = 2^{(1/5)}$$
$$= 1.149$$

~~How long would it take~~
What interest rate doubles \$
in 5 yrs? 14.9%