

6. In January 2005 there was considerable concern about the possibility of an influenza outbreak, especially because of a shortage of vaccine. An article "Influenza activity is normal" by Leanne Libby appeared in the Corpus Christi Caller-Times on January 22, 2005. For the purpose of this question, assume that the influenza in Corpus Christi can be modeled by the basic SIR model from the text.

a) (5 points) The subtitle of that article was '11 case per week in Corpus Christi.' Circle the mathematical statement that best represents that subtitle. In all cases, assume $\Delta T = 1$ week.

$$\underbrace{A}_{A}\Delta S = -11$$

$$\underbrace{A}_{B}\Delta I = -11$$

C. b = 1/11

D. $\Delta R = 11$

E. $\Delta I = 11$

b) (3 points each) The article included four tips from the Centers for Disease Control and Prevention that were supposed to help prevent flu. For each of the tips, identify the factor in the formula for 'a' that is directly changed by having people follow that tip:

A. Cover nose and mouth with a tissue when you cough or sneeze; throw tissues away after use.

Factor: Chance infection/ # contacts

B. Wash hands often with soap and water, especially after you cough or sneeze. If you are not near water, use an alcohol-based hand cleaner.

Factor: Ch Infect

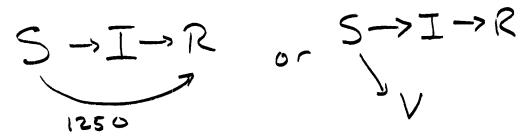
C. Stay away from people who are sick.

Factor: # contacts

D. Try not to touch your eyes, nose or mouth. Germs often spread this way.

Factor: Ch infect -s

c) (8 points) Suppose a program of vaccinating 1250 people per day for 100 days is implemented in Corpus Christi. Show a modification of the basic SIR diagram that represents this vaccination program. You do not need to write the Delta equations for the model.



7. Consider the following two-species model:

$$\frac{\Delta x}{\Delta t} = 0.6x - 0.002x^2 - 0.004xy, \qquad \frac{\Delta y}{\Delta t} = -0.75y + 0.0015xy$$
a) (6 points) Is either species logistic? How can you tell?

x is logistic. It has a squared term

b) (6 points) Is this a predator prey model or competing species model? How can you tell?

Predator Prey. X (the prey) has a negative interaction coeff. y's is positive,

c) (6 points) If the starting populations are x = 100 and y = 100, will the species x and y increase or decrease in the near future?

 $\Delta X = .6(100) - .002(100)^{2} - .004(100)(100) = 0$ $\Delta Y = -.75(100) + .4015(100)(100) = -.75 + 15 = -60$ ix stays the same. y will decrease.

d) (7 points) Find the equilibrium points for this model.

Solve DX = 0 & Dy=0 simultaneously ΔK = 0

$$-.75 + .0015 \times = 0 \times = 300$$

$$-.75 + .0015 \times = 300$$

$$-.75 + .0015 \times = 300$$

X=0 0 = 100. - 1002 x - 0. 002 x = 0 X= 16 = 300 (300,0)

x=500 => 4<0

8. Below is the phase plane for a pair of species X and Y. In Region I, it is known that $\Delta X > 0$ and $\Delta Y > 0$. is an equilibrium point.

a) (5 points each) Draw arrows to show the direction of change of the points in Region II and Region III.

b) (15 points) Interpret the phase plane biologically.

